

## Calculus (Spring) Sheet 1

1. Solve the differential equations

(a)  $y'' - 2y' + 17y = 0$

(b)  $y'' + 4y' + 3y = 0$

(c)  $y'' + 2y' = 0$  subject to  $y(0) = 3$  and  $y'(0) = -2$

2. Solve the differential equations

(a)  $y'' - 6y' + 9y = x$

(b)  $y'' - 4y' + 8y = e^{5x}$

(c)  $y'' + 2y' + 2y = \sin 3x$

(d)  $y'' + 6y' + 8y = 3e^{-2x}$  subject to  $y(0) = 1$  and  $y'(0) = -3$

3. The charge  $q$  on a capacitor in a certain electrical circuit satisfies

$$L \frac{d^2q}{dt^2} + R \frac{dq}{dt} + \frac{1}{C}q = E$$

where  $L$ ,  $R$ ,  $C$  and  $E$  are constants. Show that if  $2L = CR^2$  the general solution of this is

$$q = e^{-t/(CR)} \left( A \cos \frac{t}{CR} + B \sin \frac{t}{CR} \right) + CE$$

Please hand your work in at the lecture on Wednesday 24th February. The lecture on Monday 22nd February will be used as a tutorial.